

In the version of this article initially published, the optimality proof of the constrained algorithm for drug choice ('Constrained (cost-adjusted) algorithm for drug choice', Methods) was valid only for $N_{Resistances} = 2$. To prove for any $N_{Resistances} \geq 2$, similarly, we first assume that there exists an alternative solution K_{alt}^m that has the same distribution of drug usage but with a lower overall probability of mismatched treatment. The solutions K_{alt}^m and K_{rec}^m have the same overall number of uses of each drug $\{K_{alt}^1, \dots, K_{alt}^{N_{samples}}\} = \{K_{rec}^1, \dots, K_{rec}^{N_{samples}}\}$, and therefore

$\sum_{m=1}^{N_{samples}} C_{K_{alt}^m}^{target} = \sum_{m=1}^{N_{samples}} C_{K_{rec}^m}^{target}$. In addition, for any sample m , by definition $Q_{K_{rec}^m}^m = \min_k(Q_k^m)$, and so $Q_{K_{alt}^m}^m \geq Q_{K_{rec}^m}^m$. Finally, as $P_k^m = Q_k^m - C_k^{target}$ for any sample m and any antibiotic k , we get that the overall probability of mismatched treatment of K_{alt}^m is equal or higher than the overall probability of mismatched treatment of K_{rec}^m :

$$\sum_{m=1}^{N_{samples}} P_{K_{alt}^m}^m = \sum_{m=1}^{N_{samples}} (Q_{K_{alt}^m}^m - C_{K_{alt}^m}^{target}) = \sum_{m=1}^{N_{samples}} Q_{K_{alt}^m}^m - \sum_{m=1}^{N_{samples}} C_{K_{alt}^m}^{target} \geq$$

$$\sum_{m=1}^{N_{samples}} Q_{K_{rec}^m}^m - \sum_{m=1}^{N_{samples}} C_{K_{rec}^m}^{target} = \sum_{m=1}^{N_{samples}} (Q_{K_{rec}^m}^m - C_{K_{rec}^m}^{target}) = \sum_{m=1}^{N_{samples}} P_{K_{rec}^m}^m$$

Thus, K_{rec}^m is optimal.